## Math 10-11 Summer Packet

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1 Directions - Simplify the expression so all exponents are positive.
$b^{5} x^{-9} y^{7}=$ $\square$

2 Directions - Simplify the expression so all exponents are positive.

$$
\frac{x^{-2}}{y^{-6}}=\square
$$

3 Completely simplify the following exponential expression $\frac{36 x^{5} y^{-3} z}{-9 x^{8} y^{2} z^{4}}$ with no negative exponents.
$\square$

4 Simplify: $\frac{2 y^{2}}{4 y^{4} \cdot 2 y^{3}}$
(A) $\frac{x y^{2}}{16}$
(B) $\frac{1}{y^{6}}$
(C) $\frac{y^{2}}{6}$
(D) $\frac{1}{4 y^{5}}$

5 Directions - Simplify the expression so all exponents are positive.

$$
-4 d^{-3}=\square
$$

6 Simplify: $\left(x^{-2} y^{-3}\right)^{2} \cdot 2 x y^{2}$
(A) $\frac{y^{13}}{8 x^{13}}$
(B) $\frac{2}{x^{3} y^{4}}$
(C) $\frac{1}{8 y^{21}}$
(D) $64 x^{20} y^{4}$

7 Simplify: $x^{2} y^{2} \cdot 4 x^{4} y^{-1} \cdot x^{3} y^{-4}$
(A) $9 x^{3}$
(B) $\frac{4 x^{9}}{y^{3}}$
(C) $\frac{y^{4}}{x^{3}}$
(D) $\frac{3 x^{4}}{y^{4}}$

8 Which student correctly solved this expression?
$x^{\frac{1}{3}} \cdot x^{\frac{1}{4}}$
(A) Jo says the answer is $x^{\frac{7}{12}}$ because the exponents should be added.
(B) Kerrie says the answer is $x^{\frac{2}{7}}$ because the exponents should be added.
(C) Alex says the answer is $x^{\frac{7}{12}}$ because the exponents should be multiplied.
(D) Tracy says the answer is $x^{\frac{1}{12}}$ because the exponents should be multiplied.

9 Simplify the Expression: $\left(2 x^{5} y^{2}\right)^{3}$
(A) $2 x^{15} y^{6}$
(B) $8 x^{15} y^{6}$
(C) $8 x^{8} y^{5}$
(D) $6 x^{15} y^{6}$
$\square$

11 Solve the following equation for the given variable.
$-2(3 y-6)+4(5 y-8)=92$
(A) $y=-8$
(B) $y=6$
(C) $y=-6$
(D) $y=8$

12 Simplify: $\frac{x^{-3} y^{-4} \cdot x^{2} y^{3}}{\left(y^{3}\right)^{-4}}$
(A) $\frac{x^{4} y^{4}}{256}$
(B) $\frac{y^{11}}{x}$
(C) $\frac{x^{3}}{128 y^{10}}$
(D) $\frac{2 x^{5}}{y^{5}}$

13 Use the distributive property to solve the following equation:
$z+4(2 z+3)=15$
(A) $z=4$
(B) $\mathrm{z}=\frac{1}{3}$
(C) $z=3$
(D) $z=-1$

14
Solve the following rational equation for x .
$\frac{\mathrm{x}+2}{3}=\frac{2 \mathrm{x}-4}{2}$
$\mathrm{x}=\square$

15 Solve the equation: $5(2 x+1)=25$
(A) $x=-2$
(B) $x=-1.5$
(C) $x=1.5$
(D) $x=2$

16 Amelia bought a t-shirt for $\$ 15$ and 3 pairs of pants. She spent a total of $\$ 117$. Which equation matches this problem?
(A) $15 x+3=117$
(B) $15+3 x=117$
(C) $15 x+3 x=117$
(D) $15=117+3 x$

17 Solve the following equation:
$\frac{1}{2}(b+2)+3 b=-1$
$\square$

18 Solve the equation: $\mathbf{2 ( x + 2 x ) = 3 6}$
(A) $x=-18$
(B) $x=18$
(C) $x=-6$
(D) $x=6$

19 Factor $9 x^{2}-30 x+25$
(A) $(3 x+5)(3 x-5)$
(B) $(3 x-5)^{2}$
(C) $(3 x+5)^{2}$
(D) $3(x-5)^{2}$

20 When solving $|5 k+6|=39$ what two equations would we set up to allow us to get rid of the absolute value bars?
A $5 k+6=39$
B $5 k-6=-39$
c $-5 k+6=39$
D $5 k+6=-39$

21 A puppy named Bruno started out at 4 pounds and gained 1 pound every month. At how many months did Bruno weigh 10 pounds?
$\square$ months

22 What is the constant in 15-8y
(A) 15
(B) 8
(C) -8
(D) - -15

23
Solve the following equation by combining like terms:
$x+x+2+3 x-6=31$
$x=$ $\square$

24 Solve the following absolute value.
$-8=-3|x-5|-2$
(A) $x=\{-7,7\}$
(B) $x=\{-3,3\}$
(C) $x=\{3,7\}$
(D) $x=\{-7,-3\}$

25 Write an expression that represents the perimeter of the rectangle. Simplify the expression.
$2 x+3$


Perimeter $=\square$

26 Solve the inequality.
$5(2 x+4) \leq 5 x+20$
$\square$

27 Directions - Solve each equation for the variable.
5) $\frac{x}{3}+3=7$
$\square$

28 Anajah wants to find the solutions to the absolute value equation below:
$|-2 y+5|=17$

Which two equations should she use to find the solutions?
(A) $-2 y+5=17$
$-2 y-5=17$
(B) $-2 y+5=17$
$-2 y+5=-17$
(C) $-2 y+5=17$
$2 y-5=-17$
(D) $2 y+5=17$
$-2 y-5=-17$

29 Solve the following equation for $x$. If necessary leave your answer in simplified fraction form.

$$
\frac{3 x+8}{5}=\frac{1-2 x}{2}
$$

30 The coeffiecient for $\mathbf{6 m + 7}$ is $\mathbf{m}$
(A) True
(B) False

31 Select ALL the values that make the inequality true: $\mathbf{n}<-\mathbf{1 5}$
A -25
B -19

C -1
D -30
$\square$

33 Solve: $-3 x-7 \leq 11$
(A) $x \geq-2$
(B) $x \leq-\frac{1}{2}$
(C) $x \leq-2$
(D) $x \geq-6$

34 What is the difference $\left(4 x^{5}-3 x^{3}+2 x^{2}-7\right)-\left(x^{4}+2 x^{3}-4 x-3\right)$
(A) $5 x^{9}-x^{6}-2 x^{3}-10$
(B) $3 x^{5}-5 x^{3}-2 x^{2}-4$
(c) $4 x^{5}-x^{4}-x^{3}+2 x-4 x-10$
(D) $4 x^{5}-x^{4}-5 x^{3}+2 x^{2}+4 x-4$

35 Solve the equation. Show all work on your paper.
$32=4 y$
$y=\square$

36 Which polynomial has a leading coefficient of 4 and a degree of 3 ?
(A) $3 x^{4}-2 x^{2}+4 x-7$
(B) $4+x-4 x^{2}+5 x^{3}$
(C) $4 x^{4}-3 x^{3}+2 x^{2}$
(D) $2 x+x^{2}+4 x^{3}$

37 For the graph


Which compound inequalities represent the graph?

$$
\begin{aligned}
& \text { A }-3<x \leq 3 \\
& \text { B }-3 \leq x<3 \\
& \text { B } x>-3 \text { or } x \leq 3 \\
& \text { C } 3<x \leq-3
\end{aligned}
$$

38 For the graph


Which compound inequalities represent the graph?

A $-2<x \geq 1$
B $x<-2$ or $x \geq 1$
C $x \leq-2$ or $x>1$
D $x<-2$ and $x \geq 1$
E $-2<x \leq 1$

39 The system of inequalities $\left\{\begin{array}{l}x+y \leqslant-4 \\ 7 x-14 y \leq 0\end{array}\right.$ of linear inequalities?

(A) Region A
(B) Region B
(C) Region C
(D) Region D

40 The inequality $|2 x-5|>8$ can be written as which two inequalities?
A $2 x-5>8$
B $2 x-5<8$
C $2 x+5<8$
D $2 x+5<8$
E $2 x-5>-8$
F $2 x-5<-8$
G $2 x+5>-8$
H $2 x+5<-8$

41
The equation of a circle is shown.

$$
x^{2}+y^{2}-10 x+8 y+16=0
$$

What is the radius of the circle?

42 A home owner's monthly gas bill is $\$ 17.15$. She paid an initial deposit of $\$ 75$ to the gas company.
How much will the home owner pay in all after 3 months of service?
(A) $\$ 92.15$
(B) $\$ 126.45$
(C) $\$ 225.00$
(D) $\$ 242.15$

43 Which of the following inequalities represents the graph below?

(A) $y \geq 2 x+3$
(B) $y \leq 2 x+3$
(C) $y>2 x+3$
(D) $y<2 x+3$

44 What is the y-intercept of the quadratic function represented below?
$f(x)=(x-10)(x+2)$
(A) -20
(B) -10
(C) -2
(D) 2
(E) 10
(F) 20

45 Given $f(x)=3 x+4$, find $f(2)$.
(A) 6
(B) 7
(C) 10
(D) 14

46 Which system of inequalities is graphed below?

(A) $\left\{\begin{array}{l}y>x+2 \\ y \geq-2 x-1\end{array}\right.$
(B) $\left\{\begin{array}{l}y>x+2 \\ y \leq-2 x-1\end{array}\right.$
(C) $\left\{\begin{array}{l}y \geq x+2 \\ y<-2 x-1\end{array}\right.$
(D) $\left\{\begin{array}{l}y \leq x+2 \\ y>-2 x-1\end{array}\right.$


Solution: $\square$

48 What values of $d$ are solutions of the equation below?

$$
|3 d|=30
$$

(A) $d=2, d=-2$
(B) $d=6, d=-6$
(c) $d=10, d=-10$
(D) $d=14, d=-14$

49 The knitting club sold 40 scarves and hats at a winter festival and made $\$ 700$ from the sales. They charged $\$ 18$ for each scarf and $\$ 14$ for each hat. If $s$ represents the number of scarves sold and $h$ represents the number of hats sold, which system of equations represents the constraints in this situation?
(A) $\left\{\begin{array}{l}40 s+h=700 \\ 18 s+14 h=700\end{array}\right.$
(B) $\left\{\begin{array}{l}18 s+14 h=40 \\ s+h=700\end{array}\right.$
(C) $\left\{\begin{array}{l}s+h=40 \\ 18 s+14 h=700\end{array}\right.$
(D) $\left\{\begin{array}{l}40(s+h)=700 \\ 18 s=14 h\end{array}\right.$


Which of the following linear inequalities matches the graph above?
(A) $y>2 x-1$
(B) $y<1 / 3 x-1$
(C) $y<3 x-1$
(D) $y>1 / 3 x-1$

51 The graph of a system of inequalities is shown.


Create the system of inequalities that is represented by the graph.
$\square$
$\square$

52 A system of equations is given.

$$
\left\{\begin{array}{l}
y+2=3(x-1) \\
y=-2 x+10
\end{array}\right.
$$

What is the solution to the system?
$\square$
$\square$

53 Solve the following absolute value equation.
$2|3 x-4|+8=6$
(A) $x=\left\{\frac{5}{3}, 1\right\}$
(B) $x=\{2,4\}$
(C) No solution
(D) $x=$ All Real Numbers

54
A system of equations is given.
$y=x^{2}-9$
$y=-2 x-1$

What is one solution to the system of equations?


55 This item has three parts.
(a) Eleanor incorrectly solves the equation $\frac{1}{2}(x+18)=4(2 x-6)-9 x$.

## Part A

Select the first equation in which Eleanor makes an error.

| Step | Equation |
| :---: | :---: |
| Given | $\frac{1}{2}(x+18)=4(2 x-6)-9 x$ |
| 1. | $x+18=8(2 x-6)-9 x$ |
| 2. | $x+18=16 x-48-9 x$ |
| 3. | $x+18=7 x-48$ |
| 4. | $66=6 x$ |
| 5. | $x=11$ |

(A) Step 1
(B) Step 2
(C) Step 3
(D) Step 4
(E) Step 5
(b)

## Part B

Create an equation to correct Eleanor's error identified in part A.
$\square$

## Part C

What is the correct solution to $\frac{1}{2}(x+18)=4(2 x-6)-9 x$ ?
$x=$ $\square$

56 The equation shown is used to find the force of gravity, $F$, between two objects, where

- $G$ is the gravitational constant,
- $m_{1}$ and $m_{2}$ are the masses of the two objects, and
- $r$ is the distance between the two objects.
$F=\frac{G m_{1} m_{2}}{r^{2}}$
Which equation correctly shows the distance between the two objects?
(A) $r=\frac{\sqrt{ } F}{G m_{1} m_{2}}$
(B) $r=\frac{\sqrt{ } G m_{1} m_{2}}{F}$
(C) $r=\sqrt{\frac{F}{G m_{1} m_{2}}}$
(D) $r=\sqrt{\frac{G m_{1} m_{2}}{F}}$


Sophomore Class


The histograms shown display the number of cans of food donated by students in the freshman class and the sophomore class at a school.
Which statement is true?
(A) The freshman class has a lesser mean number of cans donated than the sophomore class.

B The freshman class has the same median number of cans donated as the sophomore class.
(C) The freshman class has a greater mean number of cans donated than the sophomore class.
(D) The freshman class has a greater median number of cans donated than the sophomore class.

58 Which expression is equivalent to $\frac{45 m^{-6} p^{2} v^{12}}{15 m^{-2} p^{8} v^{-4}}$ all values of $m, p$, and $v$ where the expression is defined?
(A) $\frac{3 v^{8}}{m^{8} p^{6}}$
(B) $\frac{3 v^{16}}{m^{4} p^{6}}$
(C) $\frac{30 m^{3}}{p^{4} v^{3}}$
(D) $\frac{30 v^{3}}{m^{3} p^{4}}$


60 Identify each part of the circle given the equation.
$(x-6)^{2}+(y-9)^{2}=225$
Center : ( $\square, \square$ )
Radius: $\square$

61 The equation of a circle is shown.
$x^{2}+y^{2}-10 x+8 y+16=0$
What is the radius of the circle?
$\square$

62 A circle is represented by the equation shown.

$$
(x-1)^{2}+(y-2)^{2}=4
$$

Which graph best represents this circle?
(A)

(B)

(c)

(D)


63 What is the equation of a parabola with vertex $(-5,6)$ and $a=3$
(A) $y=3(x+5)^{2}-6$
(B) $y=3(x+5)^{2}+6$
(C) $y=5(x-3)^{2}-6$
(D) $y=3(x-6)^{2}-5$

64 If $\mathrm{y}=-\mathrm{x}^{2}-8 \mathrm{x}-20$ is the equation of a parabola. Find the the $\mathrm{x}-$ coordinate of the vertex of parabola.
Answer: $\square$

65 What is the equation of a parabola with vertex $(-5,6)$ and $a=3$
(A) $y=3(x+5)^{2}-6$
(B) $y=3(x+5)^{2}+6$
(c) $y=5(x-3)^{2}-6$
(D) $y=3(x-6)^{2}-5$

66 Use the definition of a parabola as the set of points in the xy-plane that are the same distance from a point $F$, called the focus, and a line $d$, called the directrix, to find the equation of a parabola with focus $(0,1)$ and directrix $y=-1$.
$\square$

The equation of a parabola is $y=x^{2}+4 x+16$. Write the equation in the vertex form.
$\square$

68 Write the equation of a parabola with focus $(-3,9)$ and directix $x=0$.

Start equation with $\mathrm{x}=0$.
$\square$

69 A parabola has its vertex at $(2,-3)$ and its y-intercept at $(0,5)$.
Write an equation of the parabola in the form $y=a(x-h)^{2}+k$

$$
y=\square
$$

70 Label the x-intercept, y-intercept, vertex and axis of symmetry in the following graph


71 The directrix of the parabola $12(y+3)=(x-4)^{2}$ has the equation $y=-6$. Find the coordinates of the focus of the parabola.
$\square$

72 Which is the equation of the parabola with focus $(2,5)$ and directrix $y=3$ ?
(A) $y=-\frac{1}{2} x^{2}-x+\frac{5}{2}$
(B) $y=-x^{2}+5 x-20$
(C) $y=\frac{1}{4} x^{2}-x+5$
(D) $y=\frac{1}{2} x^{2}+x+6$

73 How is this logarithm written in exponential form?
$\log _{3}(81)=x$
(A) $x^{3}=81$
(B) $3 x=81$
(C) $3^{x}=81$
(D) $x=3^{81}$

74 Simplify/condense the logarithm $\log (4)+2 \cdot \log (x)$ into a single logarithm.
$\square$

75 Solve the exponential expression to the nearest thousandth. $8\left(5^{x}\right)-14=78$
$\square$

76 Select all the solutions to the equation $\ln \left(x^{2}\right)=\ln (24-2 x)$
$\mathrm{A} e$
B 0
c -6
D 8

E 4

77 Add together the rational expressions and write your answer in simplest form...
$\frac{3 x-4}{x^{2}-9}+\frac{2 x-1}{x+3}$
$\square$

78 Use properties of logarithms to solve the equation for $x$.
$\log (5 x+3)=18$
(A) $x=\frac{21}{5}$
(B) $x=\frac{9}{4}$
(c) $x=3$
(D) $x=\frac{e^{18}-3}{5}$
(E) $x=\frac{10^{18}-3}{5}$

79 Use properties of logarithms to solve the equation for $x$.
$\log _{2}(x+3)-\log _{2}(x+7)=2$
(A) No solution.
(B) $x=0$
(c) $x=1$
(D) $x=-\frac{7}{6}$
(E) $x=-\frac{25}{3}$

80 Change the following exponent into a logarithm $64=4^{3}$
(A) $\log _{3} 4=64$
(B) $\log _{4} 64=3$
(C) $\log _{64} 3=4$
(D) $\log _{4} 3=64$

81 What would be the remainder for the polynomial division $\left(3 x^{3}-x^{2}-7 x+6\right) \div(x+2)$
(A) -8
(B) -4
(C) 0
(D) 8

$$
\left(2 x^{3}+7 x^{2}-x-3\right) \div(x-1)
$$



83 Complete the division problem using synthetic division.

$$
\left(3 x^{4}+2 x^{3}-9 x^{2}-10 x-8\right) \div(x-2)
$$



$$
=\square x^{3}+\square x^{2}+\square x+\square
$$

85 Use synthetic division to divide $6 x^{3}-10 x^{2}+20$ by $x+1$.
(A) $6 x^{2}-16 x+16+\frac{4}{x+1}$
(B) $6 x^{2}-x+16+\frac{6}{x+1}$
(C) $6 x^{2}-16 x+16-\frac{4}{x+1}$
(D) $6 x^{2}-16 x-16+\frac{5}{x+1}$

86 Tiana is told to carry out the following polynomial division: $\left(2 x^{3}+4 x^{2}-9 x-18\right) \div(x+5)$

Quotient (Answer without remainder)
Remainder (written as a fraction)


